

Thermochemical equations – and $PV = nRT$

Lesson 9

1) Density is given as mass / volume

a) Using the equation $PV = nRT$ obtain an expression for the density of a gas.

Refer to the link above for transformation of the ideal gas equation.

$$\Rightarrow PV = nRT$$

$$\Rightarrow PV = (m/M)RT = mRT/M$$

$$\Rightarrow PM = mRT/V = PM = dRT \text{ ----- Where } d = m/V \text{ density (g/L)}$$

$$\Rightarrow d = PM/RT$$

b) What is the density, in g / mL, of Cl_2 gas at $120.00^\circ C$ and 1.00 atm pressure?

Step 1 change the units

$$\Rightarrow T = (120.00 + 273) = 393^\circ K,$$

$$P = (1.00/0.987) \times 100 \text{ kPa} = 101.3 \text{ kPa, Check conversions from Data Booklet}$$

$$M(Cl_2) = 71.0 \text{ g}$$

$$\Rightarrow d = 101.3 \times 71.0 / (8.31 \times 393) = 2.20 \text{ g/L} = 2.20 \times 10^{-3} \text{ g/mL}$$

c) The propane gas cylinder, shown on the right, was left outside at a temperature of $40.0^\circ C$. If the container was full of propane, as per label, what was the pressure exerted on the walls of the container by the propane gas if the cylinder has a volume of 9.00 litres? Assume all the propane is in the gaseous state.



Step 1 Find the mol of propane

$$\Rightarrow 3900 \text{ g} / 44.1 = 88.435$$

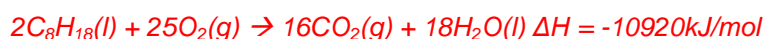
Step 2 Calculate the pressure in kPa

$$\Rightarrow P = nRT/V$$

$$\Rightarrow P = 88.435 \times 8.31 \times 313 / 9.00$$

$$\Rightarrow P = 2.6 \times 10^4 \text{ kPa (2 sig figs as the mass of propane is given to 2 sig figs)}$$

2) a) Write a balanced thermochemical equation for the complete combustion of liquid octane.



Molar heat of combustion of octane is obtained from the Data Booklet at 5460 and double since two mol of octane is shown to combust in the equation. Note the molar heat of combustion given in the Data Book assumes that water is in the liquid state.

b) When an unknown amount of octane burns completely in excess oxygen 54.64 kJ of energy is released. What volume of carbon dioxide is produced at $100^\circ C$ and at a pressure of 150.0 kPa?

Step 1 find the mol of CO_2 produced when 54.64 kJ of energy is released.

\Rightarrow Apply the ratio as per the equation

$$\Rightarrow \text{mol of } CO_2 / \text{energy} = 16 / 10920 = n / 54.64$$

$$\Rightarrow n = 8.006 \times 10^{-2} \text{ mol}$$

Step 2 Calculate the volume of CO_2

$$\Rightarrow V = nRT/P = 0.08006 \times 8.31 \times 373 / 150.0 \text{ kPa} = 1.65 \text{ L (3 sig figs)}$$

c) What mass of octane must undergo complete combustion in order to produce 4.00×10^3 litres of carbon dioxide at 100°C and 1.20 atm pressure?

Step 1 – Calculate the mol of CO_2 produced

$\Rightarrow n = PV/RT$ (Convert all units. Use the Data book)

$\Rightarrow n = 121.6 \times 4.00 \times 10^3 / (8.31 \times 373) = 156.9 \text{ mol}$

Step 2 Apply the stoichiometric ratio, as per equation, to find the mol of octane that must have reacted.

$\Rightarrow (2/16) \times 156.9 = 19.61 \text{ mol}$

Step 3 Find the mass of octane.

$\Rightarrow m = F_m \times \text{mol} = 114.23 \times 19.62 = 2.24 \text{ kg of octane (3 sig figs)}$

d) i. What amount of energy is released in, MJ, if octane burns in excess oxygen to produce 1.84×10^4 litres of CO_2 gas at SLC.

Step 1 Find the mol of carbon dioxide that is produced

\Rightarrow Since it is at SLC we can apply the formula $n_{\text{carbon dioxide}} = 18400 / 24.8 = 741.9 \text{ mol}$

Step 2 Find the energy produced in kJ

\Rightarrow Apply the stoichiometric ratio as per equation

$\Rightarrow 16/10920 = 741.9/\text{energy}$

$\Rightarrow \text{energy} = 741.9 \times 10920/16 = 5.06 \times 10^5 \text{ kJ} = 506 \text{ MJ (3 sig figs)}$ (conversion of kJ to MJ is given in the Data booklet.

ii. Give the amount of energy produced in MJ per litre of CO_2 produced.

$506 / (1.84 \times 10^4) = 2.75 \times 10^{-2} \text{ MJ/L}$